SOME CONVERGENCE RESULTS RELATED TO A STABLE BRANCHING RANDOM WALK

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Abstract: Consider a discrete-time branching random walk (V(x)) in the boundary case, where the associated random walk is in the domain of attraction of an α -stable law with $1 < \alpha < 2$. The convergence of the derivative martingale D_n is proved. Let M_n be the minimal position of (V(x)) at generation n. An integral test to describe the lower limit of $M_n - \frac{1}{\alpha} \log n$ and a law of iterated logarithm for the upper limit of $M_n - (1 + \frac{1}{\alpha}) \log n$ are established. Meanwhile, the converging rate of the additive martingale W_n is obtained. (This is based on two joint works. One is with H. He, J. Liu and the other is with J. Liu).