## HARMONIC MOMENTS AND LARGE DEVIATIONS FOR SUPERCRITICAL BRANCHING PROCESSES WITH IMMIGRATION

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**Abstract**: Let  $Z_n$  be a supercritical branching processes with immigration, we study the convergence rates of the harmonic moments of  $Z_n$ , namely,  $E(Z_n^{?r}|Zn>0)$ , r>0, extending the previous results for non-immigration cases in literatures. As a by-product, the large deviations for  $Z_{n+1}/Z_n$  are also studied. We can see that there is a phase transition in converging rates depending on the generating functions of both branching and immigration.