

# Classical and Noncommutative Martingale Inequalities

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**Abstract:** In this talk, we discuss some classical martingale inequalities and the corresponding noncommutative martingale inequalities. In particular, we present some new advances on the Burkholder-Gundy inequalities in noncommutative symmetric operator spaces.

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