Moderate Deviations for the Grenander Estimator near the Boundaries of the Support

Fuqing Gao Wuhan University, China

Hui JIANG Nanjing University of Aeronautics and Astronautics, China, E-mail: huijiang@nuaa.edu.cn

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Abstract: We investigate the asymptotic behavior of the nonparametric maximum likelihood estimator \hat{f}_n for a decreasing density f near the boundaries of the support of f. Using strong approximate and small ball estimates, a moderate deviation with explicit rate function for \hat{f}_n is established.

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