

# ON COAGULATION-FRAGMENTATION PROCESSES

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**Abstract:** The coagulation-fragmentation process describes the random aggregation and breakup of clusters of particles which can model aerosols, blood coagulation, chemical polymerization and so on. Various aspects of the processes have been extensively studied by many authors ([1]-[8]). In this talk we present mainly our works on the processes in recent years, which include the existence and uniqueness of the processes in infinite dimension, stationary distributions (invariant measure), phase transition ( gelation ) and critical value or line ([9]-[15]).

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