

# DECAY PROPERTIES OF MARKOVIAN QUEUES WITH BATCH ARRIVALS

Junping Li *The Central South University, China*

**Anyue CHEN** *The University of Hong Kong and The University of Liverpool*, E-mail: achen@hkucc.hku.hk and achen@liv.ac.uk

KEY WORDS: Decay parameter; Invariant measures; Quasi-stationary distributions; Markovian bulk-arriving queues.

MATHEMATICAL SUBJECT CLASSIFICATION: 60J27

**Abstract:** We consider the decay parameter, invariant measures and quasi-stationary distributions for a modified queueing model which stops when the queueing system is empty. Investigating such model is crucial in realizing the busy period and some other related properties of the Markovian bulk-arriving queue. In this paper, the exact value of the decay parameter  $\lambda_C$  of such model is obtained. We show that it can be easily expressed explicitly. The invariant measures and quasi-distributions of such processes are then considered. We show that there exists a family of invariant measures indexed by  $\lambda \in [0, \lambda_C]$ . We then show that under some conditions, there exists a family of, also indexed by  $\lambda \in [0, \lambda_C]$ , quasi-stationary distributions. The generating functions of these invariant measures and quasi-stationary distributions are presented. We further show that this modified queueing model is always  $\lambda_C$ -transient and some deep properties are revealed. The clear geometric interpretation of the decay parameter is explained. A few examples are then provided to illustrate the results obtained in this paper.